

welcome ^{to} back
ASTR 160

NO SCIENCE MAJORS

FRESH / SOPH
section sign-up MONDAY

JR / SR
course & sections TUESDAY
not is, noonish

1st problem set now available on
classes V2

due Thursday (START of class)

PLEASE READ P.S. POLICIES

PLEASE START EARLY

GROUPS STRONGLY ENCOURAGED

but SUBMITTED WORK SHOULD BE
YOUR OWN

HELP: sections (not this week)

+ on-line
help
sheets

office hours (CB STARBUCKS
M 9:30 - 4:00
TFs Weds TBA)

classes forum (works well)

cutoff: 8pm Weds

NEED MORE? COME TALK!

Open Yale courses

EXO PLANETS

problem: planets are too close to star

how close is it?

→ planetary orbits

$$a^3 = P^2 M$$

↗ semi-major axis
(in A.U.)

↘ orbital period (years)

↖ mass (solar masses)

↘ distance from Earth-Sun

$$a^3 = \frac{P^2 GM}{4\pi^2}$$

↖ constant depends on units

if units are
solar mass
yrs
A.U.

$$G = 4\pi^2$$

Open Yale courses

$$a^3 = p^2 M$$

$$a, M \Rightarrow p \Rightarrow (1.46 \text{ Jupiter})$$

$$\rightarrow a, p \Rightarrow M$$

$$p, M \Rightarrow a$$

Example: what is mass of Sun?

use Earth's \rightarrow mass of Sun

$$a = 1 \text{ A.U.}$$

$$p = 1 \text{ yr}$$

$$1^3 = 1^2 \times M$$

$$M = 1$$

\hookrightarrow solar masses

mks units
 \downarrow meter
 \downarrow kilogram
 \rightarrow seconds

A.U.:
 150,000,000,000

$$1 \text{ year} = 365.24 \times 24 \times 60 \times 60$$

$N \times 10^m \rightarrow \text{integer}$

\downarrow
decimal

$10^m =$
1 0 0 0 0 0
 $\underbrace{\hspace{1.5cm}}_m \text{ zeros}$

$$N \times 10^m \times A \times 10^B = A \cdot N \cdot 10^{m+B}$$

$$(N \times 10^m)^k = N^k \times 10^{m \cdot k}$$

$$(N \times 10^m)^{1/2} = N^{1/2} \times 10^{m/2}$$

$$(N \times 10^m)^{1/2} = (10 \cdot N \times 10^{m-1})^{1/2}$$

$$= (10 \cdot N)^{1/2} \times 10^{(m-1)/2}$$

$$1 \text{ AU} = 1.5 \times 10^{11} \text{ m}$$

$$1 \text{ yr} = 2.4 \times 10^7 \times 6 \times 10^4 \times 6 \times 10^4$$

$$\times 3.6524 \times 10^2 \text{ s}$$

Open Yale courses

© Yale University 2012. Most of the lectures and course material within Open Yale Courses are licensed under a Creative Commons Attribution-Noncommercial-Share Alike 3.0 license. Unless explicitly set forth in the applicable Credits section of a lecture, third-party content is not covered under the Creative Commons license. Please consult the Open Yale Courses Terms of Use for limitations and further explanations on the application of the Creative Commons license.

$$2.4 \times 6 \times 6 \times 3.6 \dots \times 10^5$$

$$\underbrace{2.4 \times 6 \times 6}_{15} \times 3.6 \dots \times 10^5$$

$$\underbrace{15 \times 3.6}_{90} \times 10^5$$

$$90 \times 10^5 = 9 \times 10^6$$

$$1 \text{ yr} = 3 \times 10^7 \text{ s}$$

in mks $G = 7 \times 10^{-11}$

P.S $a^3 = \frac{GMp^2}{4\pi^2}$

$$(1.5 \times 10^{11})^3 = \frac{(3 \times 10^7)^2 \cdot 7 \times 10^{-11} M}{4\pi^2}$$

$$(1.5 \times 1.5 \times 1.5) \times 10^{33} = \frac{3^2 \times 10^{14} \times 7 \times 10^{-11} M}{4 \times \pi^2}$$

$$= \frac{7 \times 10^4 M}{4 \times 10^1}$$

$$4 \times 10^{33}$$

$$= 2 \times 10^3 M$$

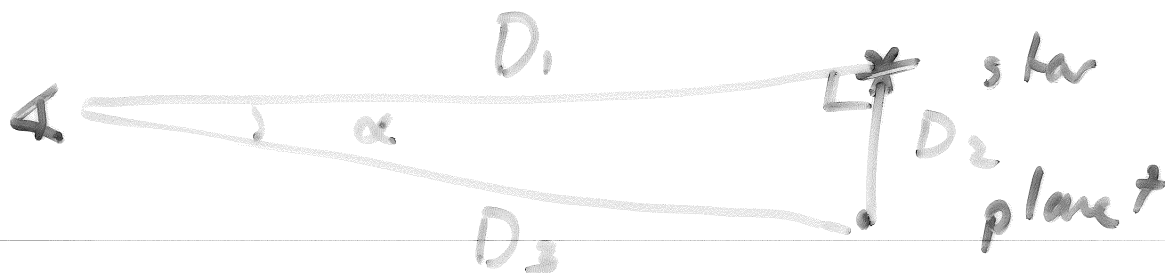
$$\frac{4}{5} \times 10^{33}$$

$$M = 2 \times 10^{30} \text{ kg}$$

$$3 = \pi = \sqrt{10}$$

NO ANDROIDS

"how close are planets
to stars"



$$\sin \alpha = \frac{D_2}{D_3}$$

Small angles
 $\sin \alpha = \alpha \rightarrow$ radians

Open Yale courses



© Yale University 2012. Most of the lectures and course material within Open Yale Courses are licensed under a Creative Commons Attribution-Noncommercial-Share Alike 3.0 license. Unless explicitly set forth in the applicable Credits section of a lecture, third-party content is not covered under the Creative Commons license. Please consult the Open Yale Courses Terms of Use for limitations and further explanations on the application of this Creative Commons license.

**SMALL ANGLE
FORMULA**

$$\boxed{\frac{D_2}{D_1} = \alpha}$$

$$\frac{D_2}{D_1} = \alpha$$

D_2, D_1 same unit

α in radians

2π radians in circle

360° in a circle

\rightarrow AU.

$$\frac{D_2}{D_1} = \alpha$$

\rightarrow arc seconds

\nwarrow
parsecs = 3×10^{16} m = 3 light years

60 arcsecs = arc minute
60 arc minutes = 1 degree

Open Yale courses

PROBLEM:

a planet with a 40 yr
period

around a star 3 pc
away

what is angular separation
 $T_{\star} \approx 10,000 \text{ K}$

HARD: plug & chug fails
because no one
equation

: missing information
(too much information)

$$P = 40 \text{ yrs} = 40 \times 10^7 \dots$$

$$D = 3 \text{ pc}$$

$$a^3 = P^2 M$$

$\hookrightarrow 1$
 $\hookrightarrow 40$

$$a^3 = 1600 = 1.6 \times 10^3$$

$$a = (1.6)^{1/3} \times (10^3)^{1/3}$$

$1 \quad 10' \quad \text{AU.}$

$$\alpha = \frac{D_2}{D_1} = \frac{10}{3} = 3.$$

$$\alpha = 3 \text{ arc seconds}$$

Light from observatory of stars is scattered over angular sizes of arcseconds

how to think about
such problems

1) have $P \Rightarrow$ want α
have D

2) suppose $M \sim M_0$

3) Ah ha $M, P \Rightarrow a$

4) distance between star-planet
is $a = D_2$

$$D = D_1$$

5) compute α

$$\alpha = D_2 / D_1$$

Open Yale courses

© Yale University 2012. Most of the lectures and course material within Open Yale Courses are licensed under a Creative Commons Attribution-Noncommercial-Share Alike 3.0 license. Unless explicitly set forth in the applicable Credits section of a lecture, third-party content is not covered under the Creative Commons license. Please consult the Open Yale Courses Terms of Use for limitations and further explanations on the application of the Creative Commons license.