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#### Name

### EVST201a/G&G 140a (2011) The Atmosphere, Ocean and Environmental Change Third Exam

Useful physical and mathematical constants:

 $R = 8314 \ J / kmole \cdot Kelvin; \quad \sigma = 5.735 \times 10^{-8} \ Wm^{-2} K^{-4}; \quad \pi = 3.14159 \ G = 6.674 \times 10^{-11} m^3 kg^{-1} s^{-2}$ 

Earth parameters:

 ${}^{'}R_{E} = 6371 km^{;} a_{E} = 0.33; g = 9.81 m/s^{2}, \Gamma = -g/c_{p} = -9.8^{\circ}C/km, Tilt=23.5^{\circ}$  $H_{s} = R_{a}T/g \approx 8.4 km; S = 1380 W/m^{2;} \Omega = 7.27 \times 10^{-5} s^{-1;} M = 5.974 \times 10^{24} kg$ 

Properties of air:  $R_{air} = 287J / kg.C; \ \rho_{air} = 1.2kg / m^3; \ C_{P_{Air}} = 1004J / kg^\circ C$ 

**Properties of water:** 

$$\rho_{water} = 1000 kg / m^{3}; \ \rho_{ice} = 917 kg / m^{3}; \ \rho_{SEA} = 1025 kg / m^{3}$$
$$L_{COND} = 2.5 * 10^{6} J / kg ; \ L_{FREEZE} = 3.34 \times 10^{5} J / kg$$
$$C_{P_{Waer}} = 4218J / kg^{\circ}C$$

**Useful definitions:**  $RH = P/P_{scat}$ ; ResTime = C/F;  $\delta D = \left[\left(\frac{D}{H}\right) / \left(\frac{D}{H}\right)_{REF} - 1\right] \times 1000$ 

Useful physical laws and balances:

$$gM = PA_{;} \quad F_{G} = \frac{GMm}{r^{2}}; \quad p = \rho RT_{;} \quad \Delta p = -\rho g \Delta Z_{;} \quad \text{Rgas} = \text{Runiversal/M}$$

$$V_{e} = \sqrt{2gR_{E}}; \quad V_{m} = \sqrt{\frac{3 RT}{M}}; \quad Q = MC_{p}\Delta T; \quad Q = L\Delta m_{v}$$

$$R = \sqrt{K \cdot T}; \quad R_{plume} = \sqrt{Kx/U};$$

$$CF = 2MU\Omega \sin\phi; \quad \tau = 0.003\rho_{A}U_{A}^{2}; \quad U_{EKMAN} = \frac{\tau}{2\rho D\Omega \sin\phi}, \quad \Delta S = S_{0}(\frac{-d}{D+d})$$

$$F = \sigma T^{4}; \quad \lambda_{m}T = 2898 \text{microns}^{\circ} K$$

$$PET(mm/month) \approx 5 \times T(C); \quad P = P_{0}e^{-Z/H}; \quad \rho = \rho_{0}e^{-Z/H_{S}}$$

$$T = \frac{4}{\sqrt{\frac{S(1-a)}{4\sigma}}}; \quad T_{GH} = T/(1-\frac{\varepsilon}{2})^{1/4}$$

$$A_{S} = 4\pi R^{2;} \quad V = (4/3)\pi R^{3}; \quad F = Scos(\varphi)^{n} \quad \Delta T = \frac{Q/A}{\rho DC_{P}}, \quad \Delta S = S_{1}(\frac{-d}{D+d})$$

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$$\begin{split} &WaterFlux = \rho_{W}UA; \ SaltFlux = S\rho_{W}UA; \ HeatFlux = C_{P}T\rho_{W}UA\\ &(\Delta p / L) \ Vol = \rho \times 2 \times \Omega \times \sin \phi \times U \times Vol\\ &PE = Mgz; \ EFF = \Delta T/T; \ Qout = K\sqrt{Zeff}, \ P(t) = P(t = 0) \exp(\gamma t)\\ &P_{Wind} = (\frac{1}{2}) \varepsilon \rho U^{3}A, \ P_{Solar} = \varepsilon S\tau_{A}Acos(\varphi), \ P_{HYDRO} = \varepsilon R\rho_{W}gzA \end{split}$$

Unit Conversions:  

$$ppmv = \frac{M_{AIR}}{M} ppmm; \ 1 \ mb = 100 \ Pascals; \ 0 \ ^{\circ}C = 273.1 \ K$$

 $1 \text{ knot} = 0.54 \text{ m/s}; \ 1 \text{ inch} = 2.54 \text{ cm}; \ ^{\circ}C = \frac{5}{9}(^{\circ}F - 32) \quad 1 \text{ tonne} = 10^{3}\text{ kg}$ 

T (°C)	P <sub>sat</sub> (mb)
-10	2.9
0	6.1
10	12.3
20	23.4
30	42.4

Molecular Weights		
$H_2$	2	
$N_2$	28	
$O_2$	32	
$CO_2$	44	
Air	29	

1. [10] Assuming that the Gulf Stream is in geostrophic balance, answer the following. If the Gulf Stream at 35N latitude is 50km wide, 1km deep and has a pressure difference across it of 4000 Pascal, compute the volumetric flow rate in the current. Express your answer in Sverdrups (i.e. 1SV= one million cubic meters per second)

- 2. [10] Consider two water masses (A and B) found near each other in the Atlantic Ocean. Mass A has S=36.0ppt and T=16C while Mass B has 35.5 and T=9C.
  - a. Determine the density of each water mass
  - b. Which water mass will be found higher in the water column?

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- 3. [10] Consider a region of the tropical Atlantic with S=35ppt. A heavy rain adds a half meter of freshwater on the ocean surface and it mixes down to 50 meters. What is the new salinity of the surface waters?
- 4. [10] In El Nino, the conditions in the eastern tropical Pacific Ocean are:

_	-	1
a.	SST	high or low?
b.	Air pressure	high or low?
c.	Precipitation	high or low?

- c. Precipitation high or low?d. Biological productivity high or low?
- e. Explain the physical connection between (a) and (d)

- 5. [10] During the last glacial maximum the conditions were
  - a. CO2 in the atmosphere h
    - high or low? land heavy or light?
  - b. Isotopes in fresh snow on Greenlandc. Oxygen isotopes in new deep sea sediments

heavy or light? high or low?

- d. Sea level
- e. Explain the relationship between (c) and (d).

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6. [10] In recent centuries, we have the perihelion in January. Explain how the climate would be different if, due to precession, perihelion occurred in June.

- 7. [10] Explain the difference between sea ice and icebergs emphasizing their origin, thickness and salinity.
- 8. [10] Compare recent trends in sea ice extent in the Arctic and Southern oceans. Be specific. In what months are they best compared?

- 9. [10] Estimate the mass of salt in the world ocean (in kg)
- 10. [10] Define
  - a. Antarctic Bottom Water
  - b. Terminal moraine
  - c. Equatorial upwelling
  - d. Mid-ocean ridge
  - e. Ekman layer